## (Part II) Lab-session 4

1) Consider the following ordered pairs of data:

| x-values: | 2 | 4 | 8 | 11 | 16 | 19 | 21 | 27 | 29 | 31 |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| y-values: | 6 | 13 | 24 | 33 | 48 | 53 | 60 | 77 | 83 | 87 |

Show that these data are linearly correlated, that is the best fit function follows

$$
\begin{equation*}
y=\alpha x+\beta . \tag{1}
\end{equation*}
$$

a) Use the SLOPE and INTERCEPT functions to determine the coefficients $\alpha$ and $\beta$.
b) Use the LINEST array function to determine the coefficients $\alpha, \beta$ and the square of the regression coefficient.
c) Produce an XY chart with trendline to determine the same quantities.
d) Compute the residues $z_{i}=\alpha x_{i}+\beta-y_{i}$. Plot the $z_{i}$-values against the $x_{i}$-values. Are the values randomly distributed? Does this plot confirm that the data are linearly correlated?
2) For the following ordered pairs of data

| x-values: | 2 | 4 | 8 | 11 | 16 | 19 | 21 | 27 | 29 | 31 |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| y-values: | 6 | 18 | 60 | 109 | 235 | 340 | 421 | 738 | 840 | 1000 |

produce an XY chart with trendline. Show that these data are correlated via a cubic equation, that is the best fit function follows

$$
\begin{equation*}
y=\alpha x^{3}+\beta x^{2}+\gamma x+\delta . \tag{2}
\end{equation*}
$$

Determine the coefficients $\alpha, \beta, \gamma, \delta$.
3) Write a subroutine called "mean" which given a set of points $\left(x_{1}, y_{1}\right),\left(x_{2}, y_{2}\right), \ldots,\left(x_{n}, y_{n}\right)$ computes the averages:

$$
\bar{x}=\frac{1}{n} \sum_{i=1}^{n} x_{i}, \quad \bar{y}=\frac{1}{n} \sum_{i=1}^{n} y_{i},
$$

and writes the values into cells C 1 and C 2 of the Excel Worksheet. In order to try your programme take the set of points of question 1). The main challenge in writing this subroutine is to have a systematic way of reading the values of $x_{i}$ and $y_{i}$ from the Excel Worksheet. Once this is achieved the sums above should be computed by means of a loop structure.
Write the values $x_{i}$ in column A and the values $y_{i}$ in column B. One way of reading these values from the Excel Worksheet is to use the command line ActiveCell.Offset (i,j).Value as was done in the last example of Lecture 4. This command line gives the value of the cell located in row $i$ and column $j$ of the Excel Worksheet. However when using ActiveCell.Offset $(i, j)$. Value your must be careful to notice that rows and columns are labelled starting at the active cell, which is then associated to row number 0 and column number 0. Write Range("A1").Select at the beginning of your subroutine so that the programme starts reading the values of $x_{i}$ at cell A1 (cell A1 is now row 0 , column 0 ).
4) If you have managed to solve question 3) successfully you may now be able to modify your subroutine so that given the same set of points it computes the slope, intercept and regression coefficient according to the formulae that were given in page 2 of Lecture 4.

