

## Mathematics for Actuarial Science: Answer sheet 3

### Sheet 5

1. (a)  $\frac{29}{4}$ , (b) 0.
2.  $y = 2x - 2$ .
3.  $-2xe^{-x^2}$ ,  $2(2x^2 - 1)e^{-x^2}$ ,  $\pm\frac{1}{\sqrt{2}}$ .
4. Max: 9, Min: 8.
5. (a)  $8x + \frac{1}{x^2}$ ,  $8 - \frac{2}{x^3}$ ,  
 (b)  $-\frac{1}{2}$ , minimum at  $(-\frac{1}{2}, 0)$ ,  
 (c)  $-\frac{1}{2}$ , 1.
6.  $27\frac{1}{2}$ .
7.  $\frac{2x-2}{x^2-2x+2}$ ,  $\frac{1}{2} \ln 2$ .
8.  $\frac{1}{4} \ln 2$ .
9.  $\frac{5}{18}$ .
10.  $\frac{1}{1+2x} + \frac{5}{(1+2x)^2} - \frac{2}{1+x}$ .
11.  $\frac{1}{3} \sin^3 x + C$ .
12.  $\frac{e^{2x}}{2} - e^x + C$ .
13.  $\frac{(4x-3)^{5/2}}{40} + \frac{(4x-3)^{3/2}}{8} + C$ .
14.  $\frac{1}{2} \tan^2 x + C$ .
15.  $-2 \cos \sqrt{x} + C$ .
16.  $\frac{(x-5)^7}{7} + \frac{8(x-5)^6}{3} + \frac{64(x-5)^5}{5} + C$ .
17.  $-\frac{1}{3} \ln |1 + \cos 3\theta| + C$ .
18.  $-\frac{1}{10} \cos 10t - \frac{1}{4} \cos 4t + C$ .
19.  $\frac{3}{8}t + \frac{1}{4} \sin 2t + \frac{1}{32} \sin 4t + C$ .

### Sheet 6

1. (a)  $\frac{1}{2}x^2 \ln x - \frac{1}{4}x^2 + C$ .
2. (a)  $\frac{2}{9}(3x+8)^{3/2} + C$ .  
 (b)  $(3x+8)e^x - 3e^x + C$ .  
 (c)  $\frac{2}{15}(3x+8)^{5/2} - \frac{16}{9}(3x+8)^{3/2} + C$ .
3.  $\frac{1}{4}x^2 - \frac{1}{2} \sin x \cos x + \frac{1}{4} \sin^2 x + C$ .
4.  $-\frac{2}{9}\pi$ .
5.  $I_n = \frac{1}{2}x^n e^{2x} - \frac{n}{2}I_{n-1}$ ,  
 $\frac{1}{4}e^{2x}(2x^4 - 4x^3 + 6x^2 - 6x + 3) + C$ .
6. (a)  $\frac{1}{3} \ln 7$ .
7. (a) 8, (b) -4, (c)  $\frac{1}{3} + 2 \ln 2$ .
8.  $\frac{7}{11}$ .
9. 0.
10.  $\frac{3}{\sqrt{10}} \tan^{-1} \left( x \sqrt{\frac{2}{5}} \right) + C$ .