MATHEMATICS: TERM 2 COURSEWORK 2

TO BE HANDED IN TO CM520 BY 4:00PM ON MONDAY 24 APRIL 2006

- 1. Using partial differentiation find $\frac{dy}{dx}$ where
 - (i) $x^2 + y^2 + x^3 y^3 = C$,
 - (ii) $(x^2 + y^2)e^{-xy} = C.$
- 2. Find all four stationary points (i.e., points where $f_x = f_y = 0$) of

$$f(x,y) = x^2y + xy^2 - x^2 - y^2 - 3xy + 2x + 2y,$$

and find their natures (i.e., are they maxima, minima or saddle points?)

- 3. Solve the following first order ordinary differential equations:
 - (i) $(4y^3 + 2x^2y + x\cos xy)\frac{dy}{dx} + 4x^4 + 2xy^2 + y\cos xy = 0.$ (ii) $\frac{dy}{dx} - x^2y^2 = 0.$
- 4. Solve the following first order ordinary differential equations:

(i)
$$\frac{d^2y}{dx^2} + 4\frac{dy}{dx} = e^{-4x} + 1$$
, $y(0) = y'(0) = 0$,
(ii) $x^2 \frac{d^2y}{dx^2} - 2x \frac{dy}{dx} - 4y = 2x^2$.

5. Evaluate the following integral using a reduction method:

$$I_n = \int_0^1 x(\ln x)^n \, dx.$$

6. Find the length of the curve $y^2 = x^3$ between x = y = 0 and x = y = 1.

Reminder: You will not be getting tables of integrals and derivatives in your examinations this year. Copies of the sheets used previously for the Mathematics I examination are available on the web page below. You are expected to know the content of these two pages.

Copies of all handouts can be found at http://www.staff.city.ac.uk/o.s.kerr/ActSciMaths/