

# Window to Viewport

Raster methods

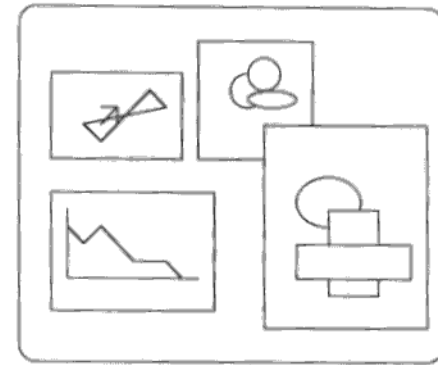
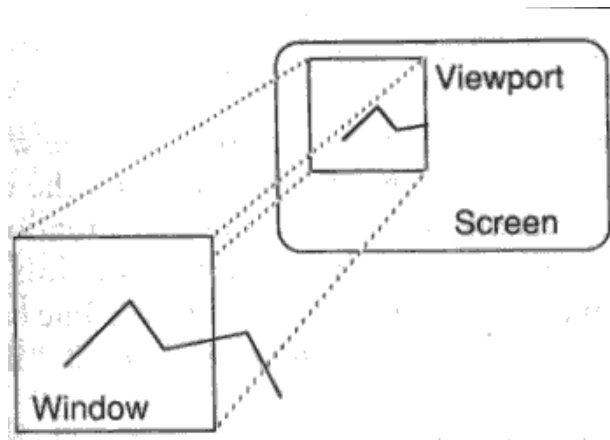
Vector methods

line clipping

polygon clipping

# Window to Viewport

- Display picture on output device

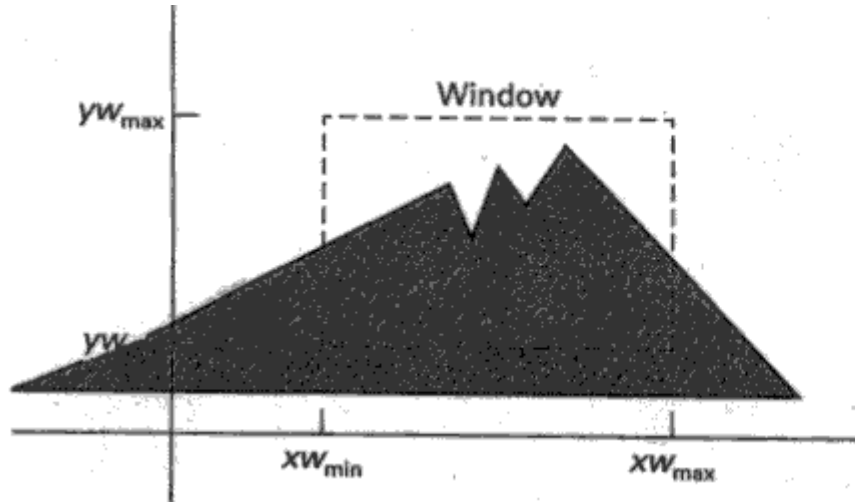


Screen showing many viewports

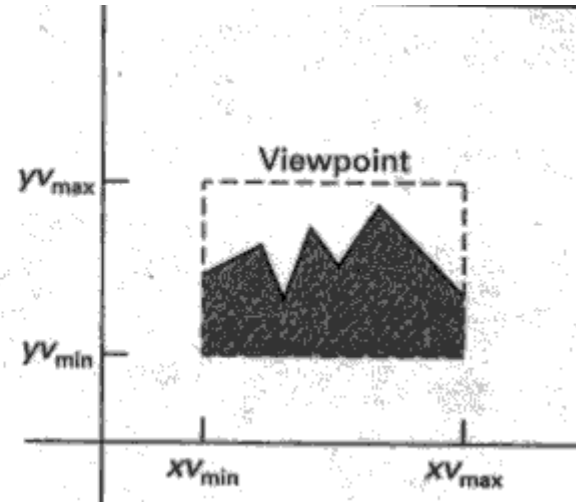
Window - area selected for display (Note not a window as in Microsoft windows) ‘what is to be viewed’

Viewport - area on display device to which window is mapped  
‘where it is to be displayed’

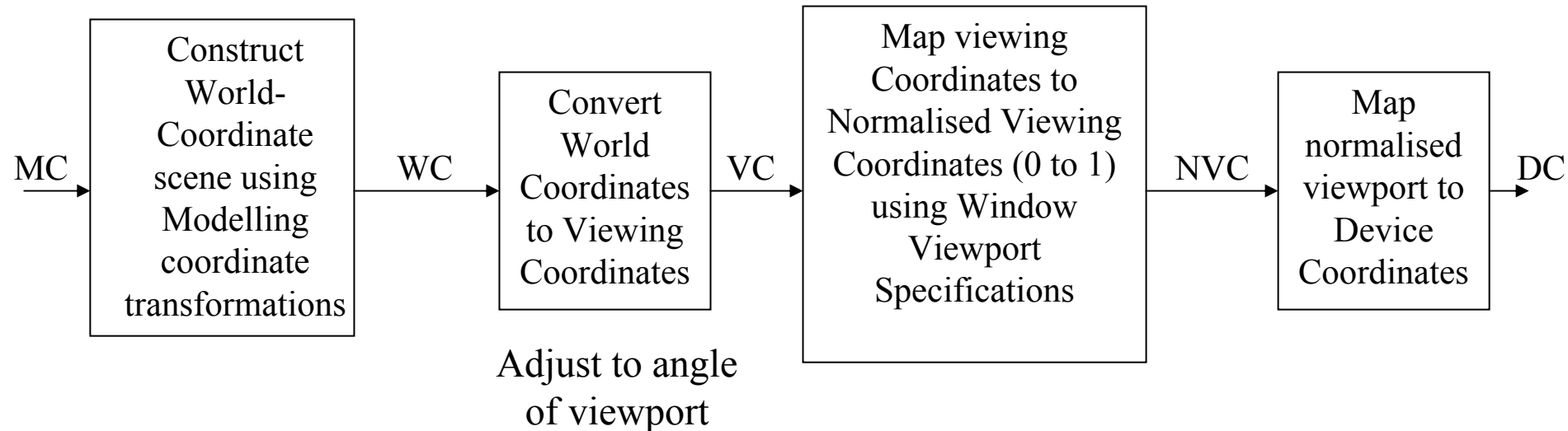
# Raster Method



World Coordinates



Device Coordinates



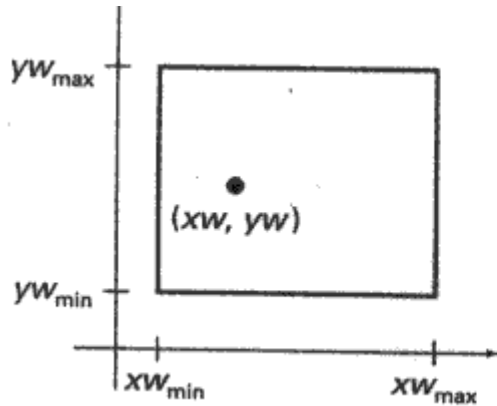
# Normalising

- Why normalise the coordinates?
  - Makes the graphics package device-independent
  - the normalised coordinates are simply mapped to the display area for the particular device in use at that time
  - different viewing devices can be used by providing the appropriate device drivers

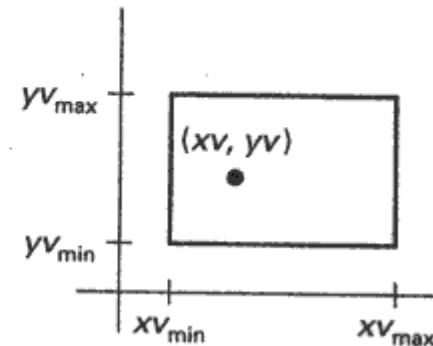
# Zoom and Pan

- Zoom
  - successively mapping different sized windows on a fixed size viewport
- Pan
  - moving a fixed size viewport across various objects in a scene

# Window to Viewpoint Mapping



Window coordinates



Viewport coordinates

To maintain relative placement in the viewport

$$\frac{xv - xv_{min}}{xv_{max} - xv_{min}} = \frac{xw - xw_{min}}{xw_{max} - xw_{min}}$$

(Similar for y coords)

The scale factor must be

$$sx = \frac{xv_{max} - xv_{min}}{xw_{max} - xw_{min}}$$

# Clipping

- Clipping applications
  - extracting part of a scene for viewing
  - identifying visible surfaces in 3D views
  - displaying a multi-window environment
  - selecting part of a picture to be edited say erased or copied.
- Clipping Algorithms covered in this module
  - Point, line, area (polygon), text

# Point Clipping

A point will be displayed if

$$xw_{\min} \leq x \leq xw_{\max}$$

and

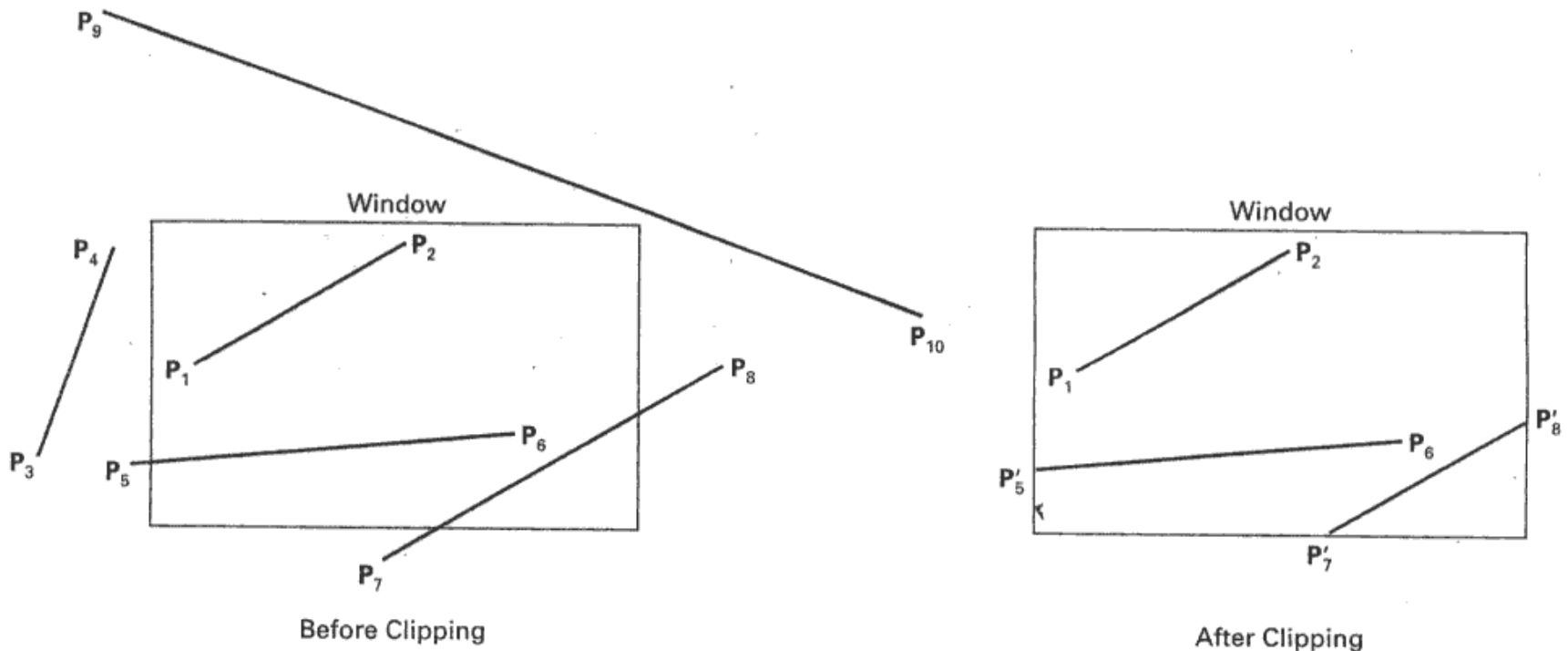
$$yw_{\min} \leq y \leq yw_{\max}$$

- Few applications
  - diagram showing particles
  - hatching for soft soil



# Line Clipping

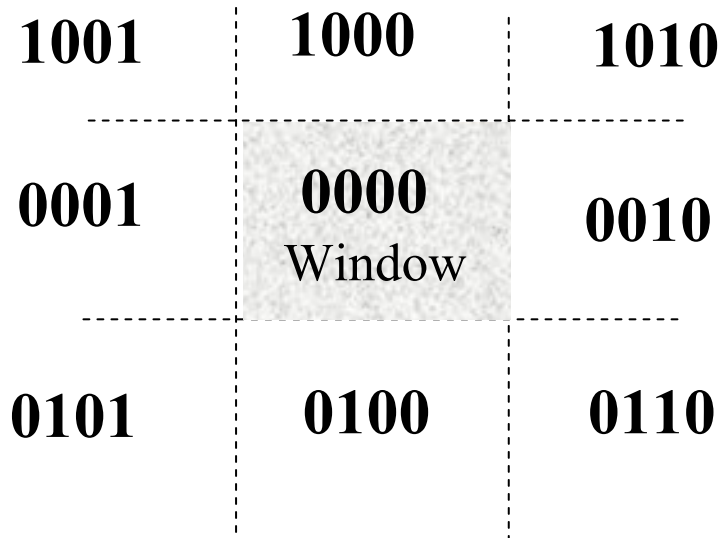
- Need an algorithm to work out
  - whether lines are in, out or across the window
  - if they cross the window, need the intersection point



# Cohen-Sutherland Line Clipping

- Step 1 - Region codes used to establish if line is in, out or across window

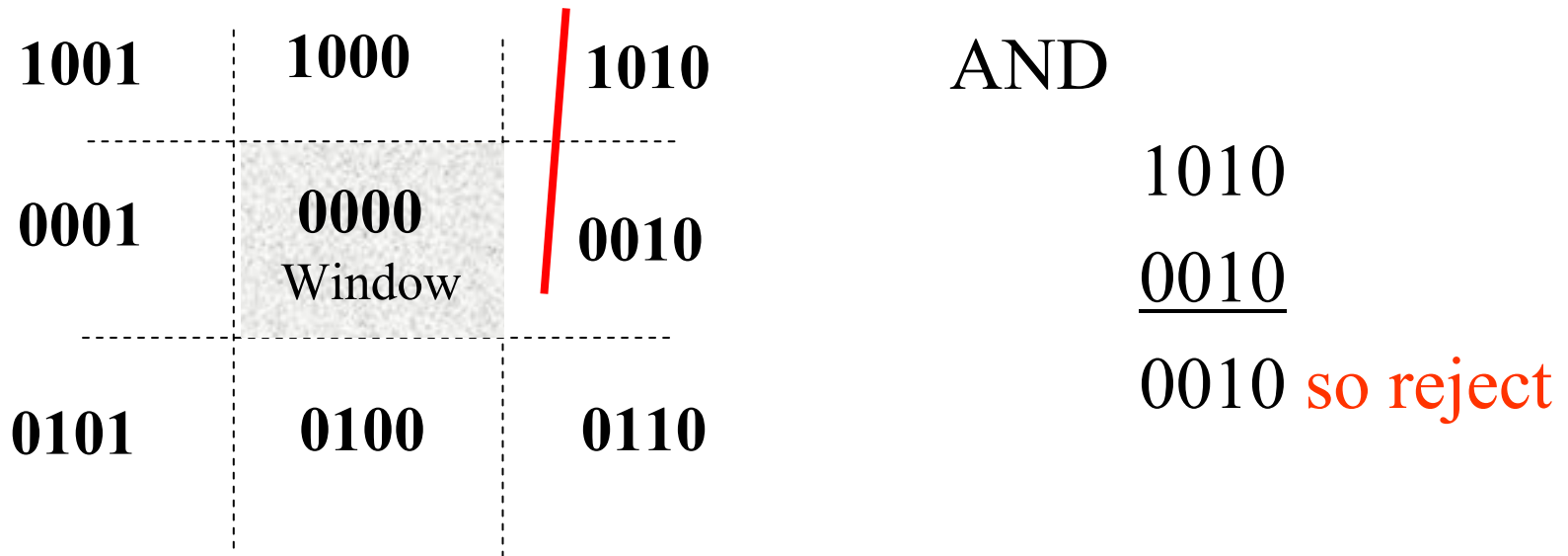
Assign line ends a binary code - on their position relative to the window.



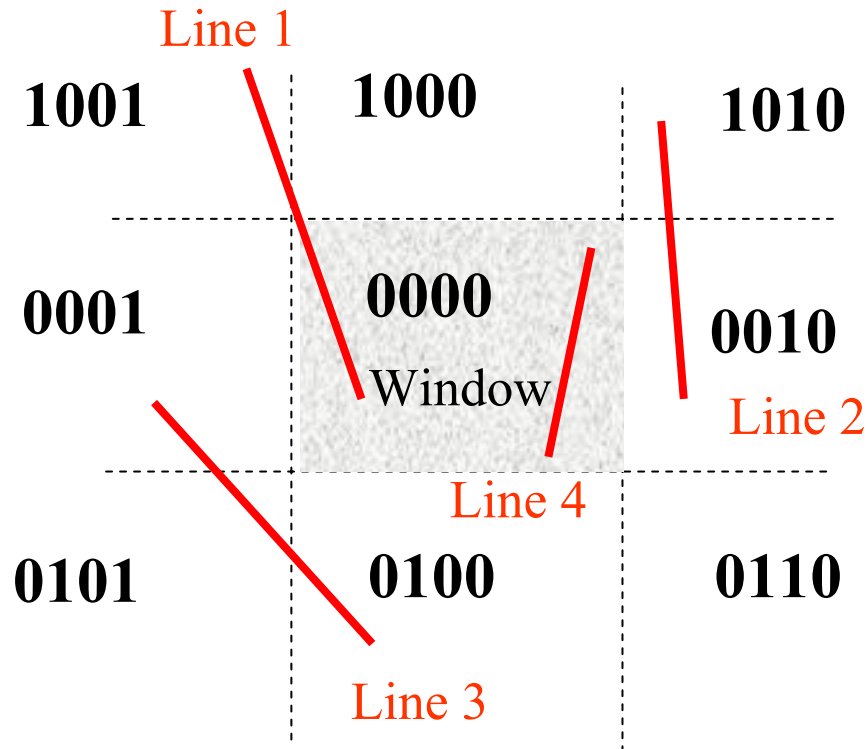
Binary (Base 2)				Position of End points
above	below	right	left	
1	0	0	0	Above
0	0	1	0	Right
0	1	0	0	Below
0	0	0	1	Left
1	0	1	0	Above and right
0	1	1	0	Below and right
1	0	1	0	Above and right
0	1	0	1	Below and left
0	0	0	0	In window

# Cohen-Sutherland 2

- Step 2 – If both lines have code 0000 - accept
- Step 3 – If AND of codes is 0000 – check for intersection
- Step 4 – Else - reject



# Practice AND



Line 1    1001  
          0000 AND  
          0000    check for  
                  intersection

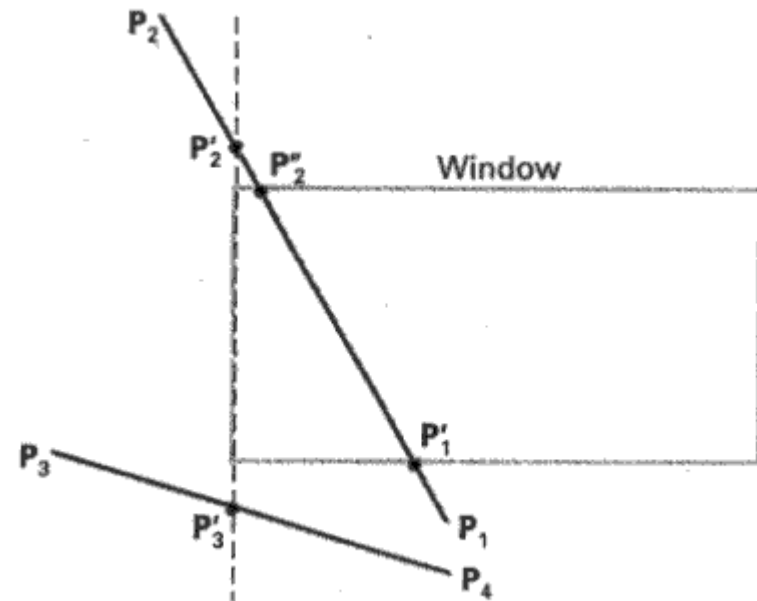
Line 2    1010  
          0010 AND  
          0010    reject

Line 3    0001  
          0100 AND  
          0000    check for  
                  intersection

Line 4    0000  
          0000  
          Both 0000 so accept

# Boundary intersections

- Checking for intersections



Consider the line  $P_1$  to  $P_2$

**$P_1$  is below the boundary.** Find intersection point  $P'_1$ . This point is on the boundary so save it.

**$P_2$  is to the left of the boundary.** Find intersection point  $P'_2$  this is outside the boundary so find point  $P''_2$ . This point is on the boundary so save it.

Save the portion of the line from  $P_1$  to  $P'_2$ .  
Repeat the procedure for  $P_3$  to  $P_4$ , reject this line

# Finding boundary intersections

- Y coordinate of intersection with vertical boundary is

$$y = y_1 + m(x - x_1)$$

Where x value is set to  $xw_{\min}$   
or  $xw_{\max}$ .  $x_1$  and  $y_1$  are the  
end point coordinates and  
 $m$ =gradient

- x coordinate of intersection with horizontal boundary is

$$x = x_1 + \frac{y - y_1}{m}$$

Where y value is set to  $yw_{\min}$   
or  $yw_{\max}$ .  $x_1$  and  $y_1$  are the  
end point coordinates and  
 $m$ =gradient

# Worked Example

A clipping window has opposite corners at 10,10 and 100,60. Show how the Cohen-Sutherland algorithm would clip a line from 20,5 to 80,20.

## **Answer**

First sketch the problem

# Worked Example cont

Codes are 0100 and 0000.

	0100	
AND	<u>0000</u>	
	0000	so part of this line may be inside the window.

Need to clip the line against the lower boundary.

$$x = x_1 + \frac{y_{\min} - y_1}{m}$$

So  $x = 20 + \frac{10 - 5}{0.25}$

So  $x = 40$

**The line would be clipped below 40,10**

Find the gradient

$$\frac{20 - 5}{80 - 20} = \frac{15}{60} = 0.25$$



# Line Clipping Problems

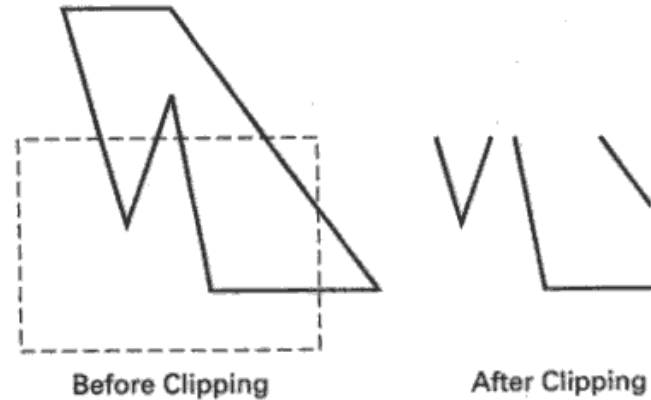
- 1 A clipping window has opposite corners at 0,0 and 20,10. Show how the Cohen-Sutherland algorithm would clip a line from 10,5 to 25, 20.(Ans 15,10)
- 2 A clipping window has opposite corners at 10,10 and 80,50. Show how the Cohen-Sutherland algorithm would clip a line from 20,20 to 100,40.(Ans 80,35)

# Polygon Clipping

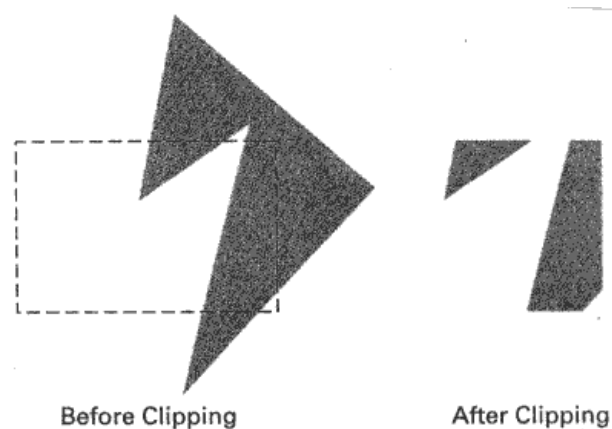
- Need to modify the line algorithm to clip polygons.

## Incorrectly clipped

Polygon clipped using line clipping Techniques.



## Correctly clipped



# Polygon Clipping

- Sutherland-Hodgeman Polygon Clipping
  - Process the polygon boundary as a whole against each window edge
  - start by clipping the polygon against the left boundary to produce a new clipped left edge for the polygon, then right, bottom and finally top
  - last step go round the sides in turn next slide



Original  
Polygon



Clip  
Left



Clip  
Right



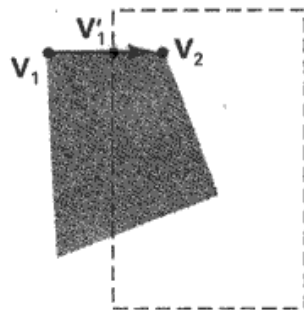
Clip  
Bottom



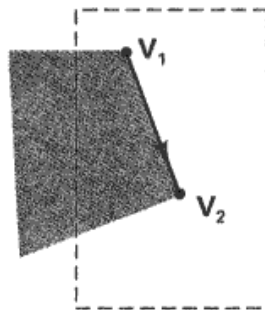
Clip  
Top

# Clipping Procedure

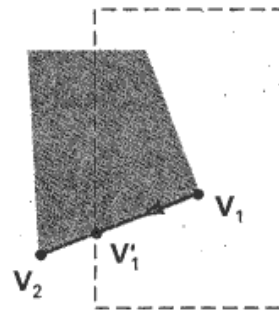
- Go round the sides in turn
  - if line goes out to in, keep intersection and and inside point
  - if line is entirely inside, keep destination point
  - if line goes from in to out, keep intersection
  - if line is entirely outside, do not keep any points



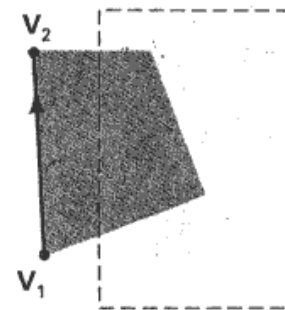
out  $\rightarrow$  in  
save  $V'_1, V_2$



in  $\rightarrow$  in  
save  $V_2$



in  $\rightarrow$  out  
save  $V'_1$



out  $\rightarrow$  out  
save none

# Clipping Example

1 to 2    out to out    keep no points

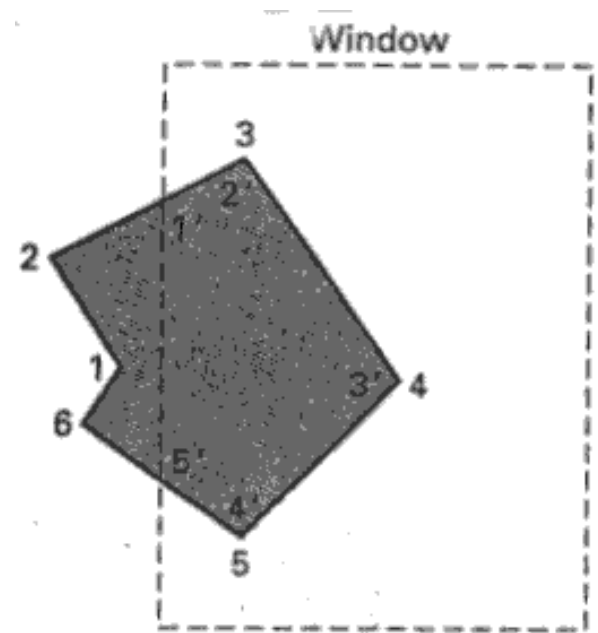
2 to 3    out to in    keep 1' and 2'

3 to 4    .....

4 to 5

5 to 6

6 to 1



Final clipped, filled shape has vertices 1',3,4,5,5'

# Polygon Clipping Problem

## Question 1

Three lines are drawn

Line 1 from 110,20 to 100,60

line2 from 100,60 to 70,40

line 3 from 70,40 to 110,20

Show how these lines would be clipped by a window having opposite corners at 20,10 and 90,80. Use Cohen-Sutherland.

Suppose these three lines formed a filled polygon. Show how the Sutherland-Hodgeman procedure would handle this polygon.

## Answer

Line 2 clipped at 90,53.3. Line 3 clipped at 30,90.

Filled polygon vertices at (90,53.3) (70,40) and (30,90)